



Foundation University  
Rawalpindi Campus

# Introduction to Database Systems – CSC - 221

A Presentation by

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# RECAP

o MY NAME IS.....

o I REMEMBER.....



**Objective of  
Today's Lecture**

**Relations and  
Relational  
Algebra**

# RDM – Two Major Strengths



**Simplicity – Relation Form**



**Strong Mathematical Foundation**



# Relational Data Model

- Presented by E. F. Codd in 1970
- Before Relational Data Model, two older data models were in use;
  - Hierarchical
  - Network

# Basics of RDM

- Mainly used for external, conceptual, and to some extent physical schema.
- Separation of conceptual and physical levels makes manipulation much easier, contrary to previous data models.

# Basics of RDM

- The basic structure is relation.
- **Relations physically represented as tables.**
- **Consists of rows and columns**
- **Both entities and relationships are modeled using tables/relations.**

# Basics of RDM

- Columns represent attributes and rows represent records.
- Rows, records and tuples all these terms are used interchangeably.



# A Table/Relation

stID	stName	clName	doB	Gender
S001	Zofeen	BCSE	12/6/92	F
S002	Rohaf	BCSE	3/9/92	M
S003	Noshail	BSCS	7/8/93	F
S004	Rameen	BCA	23/4/94	F
S005	Bilaval	BBA	22/7/93	M

# Relation - Terminology

- *Degree of a relation*: how long the tuples are, or how many columns the table has.
  - In the exemplary relation, degree of the relation is 5
- *Cardinality of the relation*: how many different tuples are there, or how many different rows the table has.
  - In the exemplary relation, cardinality of the relation is 5

# Mathematical Relations

○ Consider two sets

○  $A = \{x, y\}$

○  $B = \{2, 4, 6\}$

○ Cartesian product of these sets

○  $A \times B = \{(x,2), (x,4), (x,6), (y,2), (y,4), (y,6)\}$

# Mathematical Relations

- A relation is some subset of this Cartesian product, For example
  - $R1 = \{(x,2), (y,2), (x,6), (x,4)\}$
  - $R2 = \{(x,4), (y,6), (y,4)\}$

# Relational Model: Data Manipulation

- Data is represented as relations.
- Manipulation of data (query and update operations) corresponds to operations on relations.
- Relational algebra describes those operations. They take relations as arguments and produce new relations.
- Think of numbers and corresponding operators  $+$ ,  $-$ ,  $\setminus$ ,  $*$  or booleans and corresponding operators  $\&$ ,  $|$ ,  $!$  (and, or, not).
- Relational algebra contains two kinds of operators: common set-theoretic ones and operators specific to relations (for example projecting on one of the columns).

# Union

- Standard set-theoretic definition of union:
  - $A \cup B = \{x: x \in A \text{ or } x \in B\}$
- For example,  $\{a,b,c\} \cup \{a,d,e\} = \{a,b,c,d,e\}$
- So we require in order to take a union of relations R and S that **R and S** have the same number of columns and that corresponding columns have the same domains.

# Union – Compatible Relations

- Two relations R and S are *union-compatible* if they have the **same number of columns** and corresponding columns have the **same domains**.

# Example: Not Union Compatible

- Not Compatible!
- Different number of columns!

Anne	aaa	111111
Bob	bbb	222222
Chris	ccc	333333

Tom	1980
Sam	1985
Steve	1986



# Example: Not Union Compatible

- **Not Compatible!**
- Different domains for the second column!

Anne	aaa
Bob	bbb
Chris	ccc

Tom	1980
Sam	1985
Steve	1986

# Example: Union-Compatible

Anne	1970
Bob	1971
Chris	1972

Tom	1980
Sam	1985
Steve	1986

# Union of Two Relations

- Let  $R$  and  $S$  be two union-compatible relations. Then their union  $R \cup S$  is a relation which contains tuples from both relations:

$$R \cup S = \{x: x \in R \text{ or } x \in S\}.$$

- Note that union is a partial operation on relations: it is only defined for some (compatible) relations, not for all of them.
- Similar to division for numbers (result of division by 0 is not defined).

# Example: Shopping Lists

R

Cheese	1.34
Milk	0.80
Bread	0.60
Eggs	1.20
Soap	1.00

S

Cream	5.00
Soap	1.00

$R \cup S$

Cheese	1.34
Milk	0.80
Bread	0.60
Eggs	1.20
Soap	1.00
Cream	5.00

# Difference of Two Relations

Let  $R$  and  $S$  be two union-compatible relations.  
Then their *difference*  $R - S$  is a relation which contains tuples which are in  $R$  but not in  $S$ :

$$R - S = \{x: x \in R \text{ and } x \notin S\}.$$

- Note that difference is also a partial operation on relations.

# Example

R

Cheese	1.34
Milk	0.80
Bread	0.60
Eggs	1.20
Soap	1.00

S

Cream	5.00
Soap	1.00

R - S

Cheese	1.34
Milk	0.80
Bread	0.60
Eggs	1.20

# Intersection of Two Relations

- Let  $R$  and  $S$  be two union-compatible relations. Then their *intersection* is a relation  $R \cap S$  which contains tuples which are both in  $R$  and  $S$ :

$$R \cap S = \{x: x \in R \text{ and } x \in S\}$$

- Note that intersection is also a partial operation on relations.

# Intersection

R

Cheese	1.34
Milk	0.80
Bread	0.60
Eggs	1.20
Soap	1.00

S

Cream	5.00
Soap	1.00

$R \cap S$

Soap	1.00
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**CHHUTTI**

**AND THAT IS  
FAREWELL TO  
DAY 15 😊**